INDIAN INSTITUTE OF TECHNOLOGY, KHARAGPUR
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Department of Civil Engineering
Course: CE21003
Submission Deadline:
Total Marks:

## **Fluid Kinematics**

Q1) Consider steady, incompressible, two-dimensional flow through a converging duct. A simple approximate velocity field for this flow is

 $\overrightarrow{V} = (\mathbf{u}, \mathbf{v}) = (\mathbf{U}_0 - \mathbf{b}\mathbf{x})\,\overrightarrow{\iota} - \mathbf{b}\mathbf{y}\,\overrightarrow{j}$ 

where  $U_0$  is the horizontal speed at x=0. Note that this equation ignores viscous effects along the walls but is a reasonable approximation throughout the majority of the flow field. Calculate the material acceleration for fluid particles passing through this duct. Give your answer in two ways: (1) as acceleration components  $a_x$  and  $a_y$  and (2) as acceleration vector  $\vec{a}$ 

Q2) Consider the following steady, two-dimensional velocity field:

 $\vec{V} = (u,v) = (-0.781 - 4.67x)\vec{\iota} + (-3.54 + 4.67y)\vec{j}$ 

Is there a stagnation point in this flow field? If so, where is it?

Q3) Converging duct flow is modelled by the steady, two-dimensional velocity field of Prob.1. The pressure field is given by.

$$P = P_0 - \frac{\rho}{2} [2 U_0 bx + b^2 (x^2 + y^2)]$$

Q4) Generate an equation for the streamlines for the given velocity field.

$$\overrightarrow{V} = (\mathbf{u}, \mathbf{v}) = (\mathbf{U}_0 - \mathbf{b}\mathbf{x}) \, \overrightarrow{\iota} - \mathbf{b}\mathbf{y} \, \overrightarrow{j}$$

Q5) Generate an equation for the pathline for the given velocity field at (1,2,4).  $\vec{V} = (u, v, w) = 4x \vec{i} + (5y+3) \vec{j} + 3t^2 \vec{k}$