Propositional logic: Knight, Knave, Spy

 In an island there are three types of people - knave, knight, spy. A knight always tells the truth. A knave always lies. A spy can either tell the truth or lie. A visitor in the island meets three people A, B, and C. A says, "I am knight." B says, "I am not a spy." C says, "I am a knave." It is known that A, B, and C are of different types of people. Define the set of atomic propositions, model the problem using propositional logic, then determine the type of A, B and C.

Propositional Logic: Glasses

- You are about to leave for school in the morning and discover that you don't have your glasses. You know the following statements are true:
 - If I was reading the newspaper in the kitchen, then my glasses are on the kitchen table.
 - If my glasses are on the kitchen table, then I saw them at breakfast.
 - I did not see my glasses at breakfast.
 - I was reading the newspaper in the living room or I was reading the newspaper in the kitchen.
 - If I was reading the newspaper in the living room then my glasses are on the coffee table.
- Where are the glasses?

SAT modeling: Graph coloring

• Given a graph G = (V, E) and *n* different colors, is it possible to color the vertices of the graph using the given set of colors such that two vertices that share an edge have different colors? Find the chromatic number - minimum number of colors needed to color the vertices.

		y 3	y ₂	y 1	
	×		x ₂	x 1	
		a 3	a 2	<i>a</i> ₁	
	b_3	b ₂	b_1		
c 3	c ₂	c ₁			
Z 5	Z 4	Z 3	z ₂	Z 1	

y 3 y 2 y 1	
\times $x_2 x_1$	
$\begin{array}{c} a_3 \ a_2 \ a_1 \\ b_3 \ b_2 \ b_1 \end{array}$	$(a_3a_2a_1)_2 = (y_3y_2y_1)_2 \times x_1$ $(b_3b_2b_1)_2 = (y_3y_2y_1)_2 \times x_2$
C ₃ C ₂ C ₁	
$z_5 z_4 z_3 z_2 z_1$	

$\begin{array}{ccc} & y_3 & y_2 & y_1 \\ \times & & x_2 & x_1 \end{array}$	$(a_3a_2a_1)_2 = (y_3y_2y_1)_2 \times x_1$ $(b_3b_2b_1)_2 = (y_3y_2y_1)_2 \times x_2$	$z_1 = a_1$		
$\begin{array}{c} a_3 \ a_2 \ a_1 \\ b_3 \ b_2 \ b_1 \end{array}$		$(c_1z_2)_2 = a_2 + b_1$ $(c_2z_3)_2 = a_3 + b_2 + c_1$ $(c_3z_4)_2 = b_3 + c_2$ $z_5 = c_3$		
C ₃ C ₂ C ₁				
Z ₅ Z ₄ Z ₃ Z ₂ Z ₁		25 - 03		

SAT modeling: Circuit equivalence

• Are these two circuits equivalent?



